Abstract: We discuss how a number of very natural Markov chains, including card shuffling and the Tsetlin library, can be modeled as random walks on finite monoids and how the representation theory of these monoids can be used to compute the eigenvalues of the transition matrices of these walks. No prior knowledge about Markov chains or monoids will be assumed.