

# Temperature dependence of domain-wall bias and coercivity

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Some models for exchange bias at the interface of a ferromagnet and antiferromagnet involve the formation of partial domain walls in the antiferromagnet layer. Numerical calculations of mean-field temperature dependence are used to examine thermally induced instabilities in the partial domain wall at ideal compensated and uncompensated antiferromagnet interfaces. At compensated interfaces, depinning of the partial wall results in a total loss of bias. At uncompensated interfaces, thermal effects at the interface cause the wall to move into the antiferromagnet. The critical fields for this partial depinning are different for the forward and reverse magnetization directions. This mechanism on uncompensated interfaces allows for simultaneous loop shift and coercivity, which is not found in the compensated case. © 2001 American Institute of Physics.

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## I. INTRODUCTION

Several mechanisms of exchange bias have been proposed to explain the experimentally observed bias and coercive fields of exchange coupled ferromagnet/antiferromagnet systems since the original work by Meiklejohn and Bean.<sup>1</sup> Exchange bias can be described by a displacement of a hysteresis loop along the field axis by  $H_E \propto J_I/M_f t_f$  where  $J_I$  is the interlayer exchange between the ferromagnet and antiferromagnet,  $M_f$  is the saturation magnetization of the ferromagnet, and  $t_f$  is the thickness of the ferromagnet. The bias field is measured by taking the midpoint of the two loop intercepts on the field axis. Likewise, the coercivity is measured as half the absolute width of the hysteresis loop at the field axis.

The earliest models tended to overestimate the bias field for reasonable values of  $J_I$ . Modified mechanisms have been proposed requiring partial domain wall formation near the interface. These models apply to ideal uncompensated<sup>2</sup> and compensated<sup>3</sup> interfaces, with differences appearing in the angular dependence of  $H_E$  and spin canting the compensated interface. Domain-wall bias emphasizes a balance between an applied field  $H_a$  and wall energy  $\sigma = 2\sqrt{A_{af}K_u}$ , where  $A_{af}$  and  $K_u$  are the exchange spring and uniaxial magnetocrystalline anisotropy energies, respectively. If the partial wall becomes unstable with respect to out-of-plane fluctuations, the domain wall is depinned from the interface and results in a loss of bias.<sup>4</sup> This happens at a critical rotation angle  $\theta_c$  and also depends on an easy-plane anisotropy  $K_o$  tending to keep the spins in-plane.<sup>5</sup> Since the effective  $K_o$  is reduced by thermal fluctuations,  $\theta_c$  is also sensitive to increased temperature.<sup>6</sup>

In a mean-field approach to temperature dependence, the effective  $K_o$  above plays a role akin to an energy barrier to thermal activation.<sup>7-9</sup> While dynamic processes are important when the system is close to a transition, mean-field

theory<sup>10</sup> is very useful for studying the static features of the system away from this point. Equilibrium configurations calculated from a mean-field theory may not predict the exact critical temperatures and fields, but the approach captures the essential physics of the system before and after such a transition.

In this article, we examine the thermal stability of partial domain wall-mediated bias on compensated and uncompensated antiferromagnetic interfaces. Thermal fluctuations are shown to reduce the stabilizing effect of  $K_o$ , and induce a transition from reversible domain-wall mediated bias with no coercivity to coercive hysteresis loops having small or vanishing bias.

## II. MEAN FIELD CALCULATIONS

The stability of partial domain walls in the antiferromagnet to thermally induced transitions is examined using an atomistic model. Landau-Lifshitz equations of motion for each spin  $S_i$  at position  $i$  are constructed and solved numerically:

$$\frac{\partial S_i}{\partial t} = -\gamma(S_i \times h_i) + \alpha(S_i \times \dot{S}_i \times h_i). \quad (1)$$

The effective field  $h_i$  at each spin site contains contributions from the applied field  $H_a$  (in units of  $M_f t_f / \sigma$ ), the exchange integral between nearest neighbors  $J_{ij}$  and also uniaxial anisotropy  $K_U$  in the antiferromagnet. The ferromagnetic layer is assumed to be isotropic. The equilibrium configuration found using this method probes the out-of-plane stability and thereby avoids some difficulties with metastable configurations.

The bulk antiferromagnetic exchange integral  $J_{af}$  is chosen such that the antiferromagnet has a Néel temperature ( $T_N$ ) of 300 K and the bulk ferromagnetic exchange integral was set at  $J_f = 10J_{af}$ . Demagnetizing fields in the ferromagnet are represented by an additional term in  $h_i$  of magnitude  $4\pi S_z$ , where  $S_z$  is the component of  $S_i$  along the film normal. The gyromagnetic ratio and damping factor are  $\gamma$  and  $\alpha$ ,

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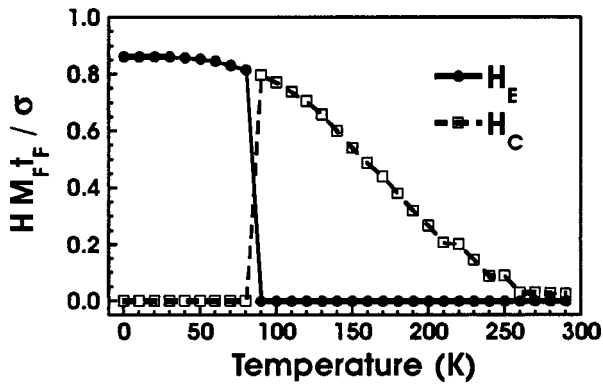


FIG. 1. Temperature dependence of bias field and coercive field for a compensated interface with  $J_I = 3J_{af}$ . The critical temperature at which bias vanishes is 90 K. Note that biased loops and coercivity do not occur simultaneously.

respectively. Spins are arranged in a simple cubic structure, with periodic boundary conditions in the [100] and [010] directions. The ratio  $J_{af}/K_u$  is chosen to give a characteristic domain wall width of about ten atomic planes and the antiferromagnet layer thickness was chosen to be large enough to accommodate the domain wall.

Temperature dependence is implemented by replacing  $h_i$  with its thermally averaged value  $\langle h_i \rangle$ , where the spin vectors  $S_i$  are reduced in size by the Brillouin function  $\langle S_i \rangle = S_i \times B(T)$ . Note that  $B(T)$  is itself a function of  $h_i$ , so  $\langle h_i \rangle$  requires iteration to self-consistency.<sup>10</sup>

### III. RESULTS AND DISCUSSION

The results presented here were calculated using  $K_o = K_u$ ,  $t_f = 10$  ML and  $t_{af} = 20$  ML. Values of  $\alpha = \gamma = 0.0002$  were used and these gave stable convergence in reasonable time. To avoid numerical problems with metastable configurations, the external field was applied at  $80^\circ$  and  $10^\circ$  to the antiferromagnet anisotropy axis for the compensated and uncompensated interface, respectively.

Equilibrium spin configurations between 0 and 290 K were calculated for  $J_I = 3J_{af}$  with an ideal compensated interface. Calculations for an ideal uncompensated antiferromagnetic interface were carried out for  $J_I = J_{af}/4$ ,  $J_{af}$  and  $3J_{af}$ .

#### A. Compensated interfaces

A minimum  $J_I/J_{af}$  ratio of at least 2 was required to obtain a stable partial domain wall at  $T = 0$  K.<sup>5</sup> Bias and coercive fields as a function of temperature for  $J_I = 3J_{af}$  on a compensated interface are shown in Fig. 1. Below  $T = 90$  K, the antiferromagnet spin configuration supports a reversible domain wall. Above  $T = 90$  K, the wall can exceed the critical angle  $\theta_c$  so depinning of the wall can occur.

Just prior to becoming unstable, the spin structure in the antiferromagnet consists of a domain wall wound through an angle close to  $\theta_c$ , with the spins away from the interface winding towards the positive anisotropy axis. When depinning occurs, the ferromagnet magnetization immediately falls to its negative saturation value as the antiferromagnet spins rotate out of the plane of the film. This allows the

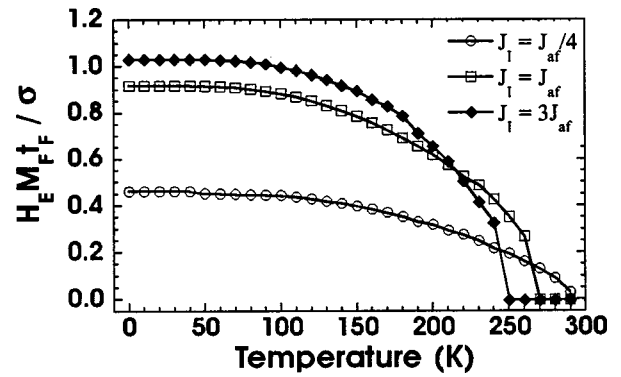


FIG. 2. Temperature dependence of the bias field for uncompensated interfaces with  $J_I = J_{af}/4$ ,  $J_I = J_{af}$  and  $J_I = 3J_{af}$ . Note that  $T_{eb}$  increases for as  $J_I$  is decreased.

domain wall to escape, and causes the system to “forget” its initial configuration in the positive direction. The spin structure after depinning is identical to the initial condition at positive saturation, except now the spins further away from the interface rotate towards the negative anisotropy axis.

When the ferromagnet magnetization is restored to positive saturation, it is as if the system had its initial condition in the negative direction. A domain wall is again wound up to angle  $\theta_c$  relative to the negative anisotropy axis, and depinning occurs as the ferromagnet is pulled into the field direction. The critical fields for depinning occur at the same magnitude in both directions. Since bias is measured as the midpoint between these critical fields, the bias field is zero.

If a  $J_I/J_{af}$  ratio of unity is used, the partial domain wall always depins from the interface during magnetization reversal. In a mean-field formulation, the temperature dependence of the coercive field has been shown to follow the Brillouin function.<sup>11</sup> The bias field is zero at all temperatures due to the perfect compensation at the antiferromagnet interface.

#### B. Uncompensated interfaces

Bias fields as a function of temperature for uncompensated interfaces with different  $J_I$  are given in Fig. 2. In the limit of  $J_I \ll \sigma$ , antiparallel alignment of spins in the antiferromagnet is only slightly perturbed. This is the case for  $J_I = J_{af}/4$ , where bias is fully reversible up to 290 K. The decrease in the bias field with temperature is due to reduction of the interface antiferromagnet  $\langle S \rangle$  as the temperature approaches  $T_N$ . Exchange bias is lost at critical temperature  $T_{eb}$  near  $T_N$ .

When  $J_I$  is increased, the bias field vanishes at a temperature  $T_{eb}$  less than  $T_N$ . At low temperatures a domain wall forms in the antiferromagnet and remains pinned to the interface as the magnetization is reversed. Above  $T_{eb}$ , partial walls in the antiferromagnet are depinned during magnetization reversal and the bias disappears.

The coercive fields have interesting temperature dependence as shown in Fig. 3. For  $J_I = J_{af}/4$  there is no coercivity, but for  $J_I = J_{af}$  and  $J_I = 3J_{af}$ , there is coercivity below  $T_{eb}$ . The coercivity begins to appear before the bias field goes to zero, and maximum coercivity occurs at  $T_{eb}$  where the bias field becomes zero. The appearance of coercivity

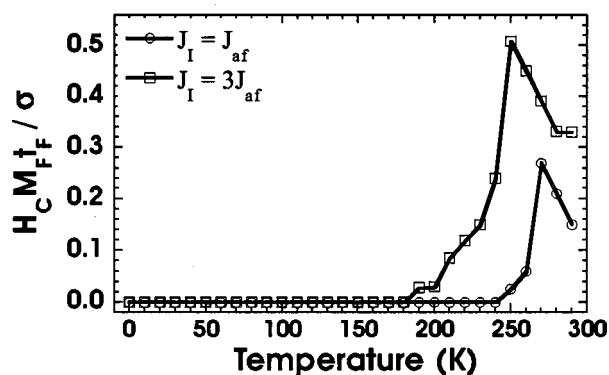


FIG. 3. Temperature dependence of the coercive field for uncompensated interfaces with  $J_I = J_{af}/4$ ,  $J_I = J_{af}$ , and  $J_I = 3J_{af}$ . The onset of coercivity occurs at lower temperatures as  $J_I$  is increased.

corresponds to differences in the thermal magnitudes of the interface antiferromagnet  $\langle S \rangle$  for the forward and reverse magnetizations. This can be understood as follows: Near  $T_N$ , the thermal magnitudes of the antiferromagnet spins can vary greatly throughout the film. This has a large influence on the structure of the partial wall formed during magnetization reversal. In particular, just before the bias field vanishes at  $T_{eb}$ , the partial wall does not entirely depin from the interface at the coercive field, but penetrates into the antiferromagnet and is centered at a depth determined by a minima in  $\langle S \rangle$  as a function of depth. This process occurs over a narrow window of temperatures just below  $T_{eb}$ .

#### IV. CONCLUSION

Results from a mean field theory for exchange bias at finite temperatures was presented for ideal compensated and

uncompensated interfaces. Pinning of partial walls to the interface was found to be sensitive to the thermally averaged magnitudes of antiferromagnet spins near the interface. The bias field was found to vanish at a critical temperature  $T_{eb}$  less than the Néel temperature. For large values of interlayer exchange, coercivity appears as the bias field vanishes. In the case of an uncompensated interface, a maximum in the coercivity occurs at  $T_{eb}$  due to partial depinning of the domain wall in the antiferromagnet.

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